

Some Practice Questions for Exam 1

Part I: Short Answer Questions

1. $\int_{-\infty}^{\infty} (\tau^2 + 1)\delta(1 - \tau)d\tau$ equals to

- a) 0 b) -2 c) 3 d) 2

2. Given that $y(t) = \int_{-\infty}^t e^{2(t-\tau)}x(\tau - 2)d\tau$ is a LTI system, its impulse response is:

- a) $h(t) = e^{2(t-2)}u(t - 2)$
b) $h(t) = e^{2(t+2)}u(t + 2)$
c) $h(t) = e^{2(t+2)}u(t - 2)$
d) $h(t) = e^{2(t-2)}u(t + 2)$

3. Determine whether the following statements are true or false.

a) The product of an even and an odd function is even.

b) $x(t) = \cos(4t + 30)$ is periodic with period π seconds.

c) $x(t) = \cos(t)u(t)$ is a power signal.

d) $y(t) = x(3t)$ is time-invariant.

4. The system $y(t) = \int_{-\infty}^{\infty} x(\tau)u\left(\frac{\tau - t}{2}\right)d\tau$ is

- a) time-varying
b) non-causal
c) BIBO stable
d) None of these

5. The inverse Laplace transform of $1 - \frac{s}{s+3}$ is

- a) $\delta(t) - e^{-3t}u(t)$
- b) $3e^{-3t}u(t)$
- c) $\delta(t) - 3e^{-3t}u(t)$
- d) $e^{-3t}u(t)$

Part II- Long Answer Questions

1. For a LTI system, it is known that when the input to the zero-state system is the unit step function the output is $y(t) = (1 - e^{-t})u(t)$.

- a) Find the impulse response of the whole system using Laplace transform.
- b) Find the impulse response of the whole system in the time domain.
- c) Find the response of the system to $x(t) = tu(t)$.

2. Consider the Circuit 2 in question 4.29 from the book.

- a) Find the zero-state response to $x(t) = 2\cos(4t)$, assume $R = 2\Omega, C = 1F$.
- b) Find the transient and the steady-state responses.
- c) Find the zero-input response assuming $y(0) = 2$