

NAME SOLUTION

ECE 202

EXAM I

JULY 14, '06

<u>PROBLEM</u>	<u>POINTS</u>	<u>SCORE</u>
1	24	_____
2	26	_____
3	26	_____
4	<u>24</u>	=====
	100	

NOTE:

- 1) YOU MUST PLACE YOUR ANSWERS ON THE LINES PROVIDED.
- 2) SOME ANSWERS MAY HAVE LITTLE OR NO PARTIAL CREDIT. PLEASE CHECK YOUR WORK.
- 3) SOME ANSWERS MAY HAVE PARTIAL CREDIT, SO PLEASE SHOW YOUR WORK.
- 4) THIS EXAM HAS 4 PROBLEMS EACH ONE PAGE LONG. CHECK TO SEE YOU HAVE 4 PROBLEMS.
- 5) ALL ANSWERS MUST HAVE UNITS AND BE IN ENGINEERING NOTATION.

1) ANSWER THE FOLLOWING

A) FIND THE PHASOR REPRESENTATIONS OF THE TIME DOMAIN FUNCTIONS

$$i) v_1 = 47 \cos(377t + 62^\circ) \text{ V}$$

$$\vec{V}_1 = \underline{47 \angle 62^\circ \text{ V}} \quad (4)$$

$$ii) i_1 = 14 \sin(2000t - 13^\circ) \text{ mA}$$

$$14 \cos(2000t - 13^\circ - 90^\circ) \text{ mA}$$

$$\vec{I}_1 = \underline{14 \text{ mA} \angle -103^\circ} \quad (4)$$

$$iii) v_2 = -881 \cos(4t - 25^\circ) \text{ V}$$

$$881 \cos(4t - 25^\circ + 180^\circ)$$

$$\vec{V}_2 = \underline{881 \angle 155^\circ \text{ V}} \quad (4)$$

B) IF $f = 770 \text{ Hz}$, FIND THE TIME DOMAIN FUNCTIONS FOR THE FOLLOWING PHASORS

$$i) \vec{I}_2 = 7 \mu + j 6 \mu \text{ A}$$

$$9.22 \mu \angle 40.6^\circ$$

$$i_2(t) = \underline{9.22 \mu \cos(4.84kt + 40.6^\circ) \text{ A}} \quad (4)$$

$$ii) \vec{V}_3 = 31 - j 21 \text{ V}$$

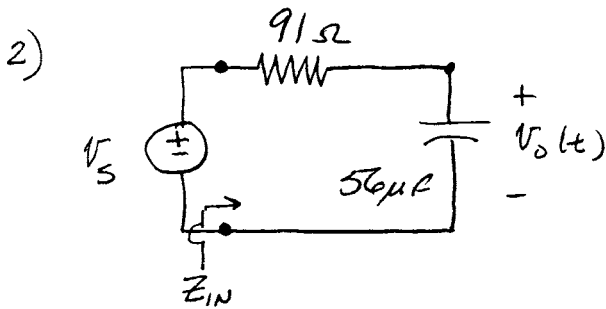
$$37.4 \angle -34.1^\circ$$

$$v_3(t) = \underline{37.4 \cos(4.84kt - 34.1^\circ) \text{ V}} \quad (4)$$

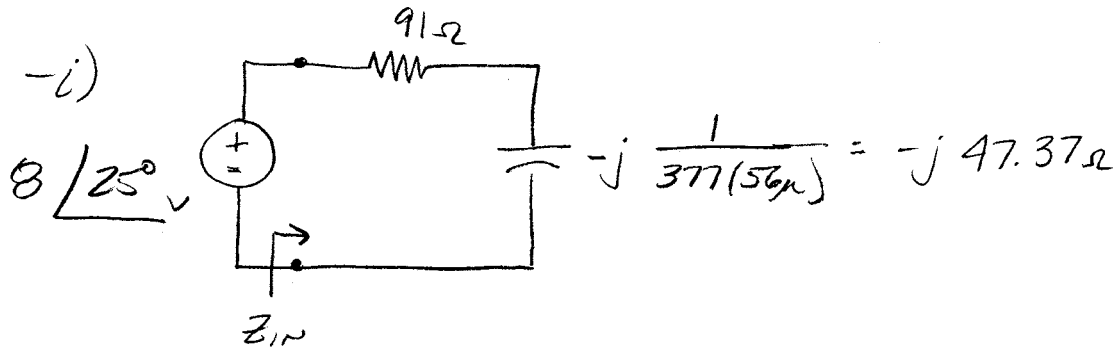
C) WHAT IS THE IMPEDANCE OF A 220 mH INDUCTANCE IF $f = 60 \text{ Hz}$?

$$j\omega L = j(377)(0.22)$$

$$Z = \underline{j 82.94 \Omega} \quad (4)$$

A) FIND Z_{IN} IN POLAR FORMB) FIND THE STEADY-STATE VOLTAGE $v_o(t)$

$$v_s = 8 \cos(377t + 25^\circ) \text{ V}$$



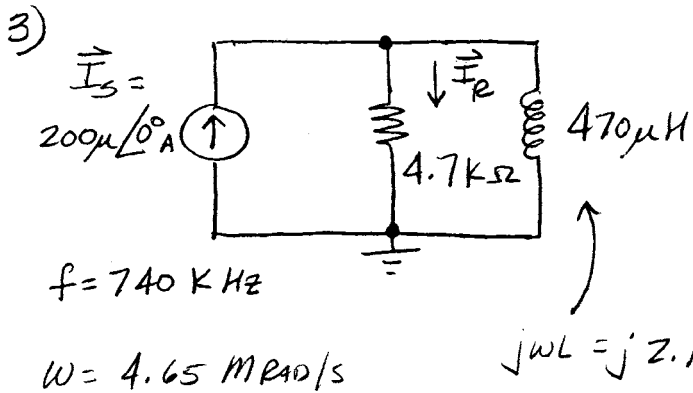
$$\text{-ii)} \quad Z_{IN} = 91 - j47.37 = 102.6 \angle -27.5^\circ$$

$$\begin{aligned} \vec{V}_o &= 8 \angle 25^\circ \frac{-j47.37}{91 - j47.37} \\ &= 8 \angle 25^\circ \frac{47.37 \angle -90^\circ}{102.6 \angle -27.5^\circ} \\ &= 3.69 \angle -37.5^\circ \end{aligned}$$

$$\text{-iii)} \quad v_o(t) = 3.69 \cos(377t - 37.5^\circ)$$

$$Z_{IN} = \underline{102.6 \angle -27.5^\circ \Omega} \quad (12)$$

$$v_o(t) = \underline{3.69 \cos(377t - 37.5^\circ) \text{ V}} \quad (14)$$



GIVEN THIS FREQ. DOMAIN
CIRCUIT, FIND \vec{I}_R ,
IN RECTANGULAR FORM,
BY USING THE
CURRENT DIVIDER RULE.

$$\vec{I}_R = 200 \mu\text{A} \angle 0^\circ \frac{j2.185 \text{ k}\Omega}{4.7 \text{ k}\Omega + j2.185 \text{ k}\Omega}$$

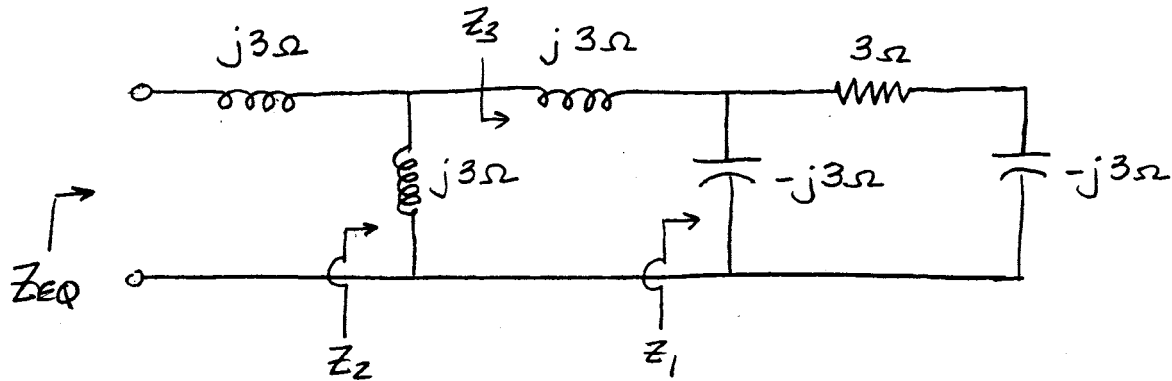
$$= 200 \mu\text{A} \angle 0^\circ \frac{2.185 \text{ k}\Omega \angle 90^\circ}{5.183 \text{ k}\Omega \angle 24.9^\circ}$$

$$= 84.3 \mu\text{A} \angle 65.1^\circ$$

$$= 35.5 \mu\text{A} + j76.46 \mu\text{A}$$

$$\vec{I}_R = \underline{(35.5 \mu\text{A} + j76.46 \mu\text{A}) \text{ A}} \quad (26)$$

- 4) GIVEN THE FREQ. DOMAIN CIRCUIT, FIND Z_1 , Z_2 AND Z_{EQ} IN POLAR FORM



$$Z_1 = \frac{-j3(3-j3)}{-j3+3-j3} = \frac{-j9-9}{-j6+3} = \frac{12.73 \angle -135^\circ}{6.71 \angle -63.4^\circ}$$

$$= 1.897 \angle -71.6^\circ = 0.598 - j1.8$$

$$Z_3 = j3 + 0.598 - j1.8 = 0.598 + j1.2$$

$$Z_2 = \frac{j3(0.598 + j1.2)}{j3 + 0.598 + j1.2} = \frac{j1.794 - 3.6}{0.598 + 4.2} = \frac{4.02 \angle 153.5^\circ}{4.24 \angle 81.9^\circ}$$

$$= 0.948 \angle 71.6^\circ = 0.3 + j0.9$$

$$Z_{EQ} = j3 + 0.3 + j0.9 = 0.3 + j3.9 = 3.91 \angle 85.6^\circ$$

$$Z_1 = 1.897 \angle -71.6^\circ \Omega \textcircled{8}$$

$$Z_2 = 948 \text{ m} \angle 71.6^\circ \Omega \textcircled{9}$$

$$Z_{EQ} = 3.91 \angle 85.6^\circ \Omega \textcircled{9}$$