

$$\frac{1}{k} \leftarrow \leftarrow \leftarrow \oplus \xrightarrow{\pm 180^\circ} L(s) = -\frac{1}{k}$$

C.E.  $1 + kL(s) = 0$

# hw 8 departure angles

Note Title

11/17/2008

#7 
$$L(s) = \frac{(s+1)}{(s+2+2j)(s+2-2j)}$$

$$\begin{cases} z_1 = -1 & \checkmark \\ p_1 = -2+2j & \checkmark \\ p_2 = -2-2j & \end{cases}$$

$$L(s) = \frac{(s-z_1)}{(s-p_1)(s-p_2)}$$

RL  $\rightarrow$  Angle condition  
test point  $s_0$

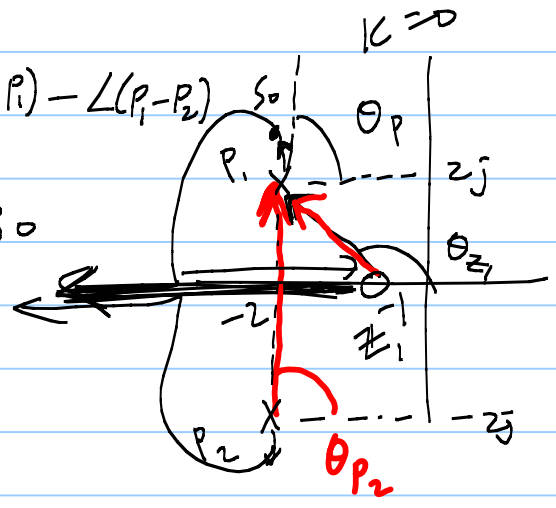
$$\angle L(s_0) = \angle(s_0 - z_1) - \angle(s_0 - p_1) - \angle(s_0 - p_2)$$

$$\underline{\underline{= \pm 180^\circ}}$$

$$\lim_{s_0 \rightarrow p_1} \angle L(s_0) = \angle(p_1 - z_1) - \lim_{s_0 \rightarrow p_1} \angle(s_0 - p_1) - \angle(p_1 - p_2)$$

$$= \theta_{z_1} - \theta_{dep} - \theta_{p_2} = \pm 180$$

$$\theta_{dep} = \pm 180 + \theta_{z_1} - \theta_{p_2}$$



$$CE \Rightarrow 1 + KL(s) = 0 \quad L(s) = -\frac{1}{k} \quad \angle \pm 180^\circ$$

hw 8

# 5

$$L(s) = \frac{1}{s(s-p_1)(s-p_2)}$$

$$P_0 = 0$$

$$P_1 = -4 + 4j$$

$$P_2 = -4 - 4j$$

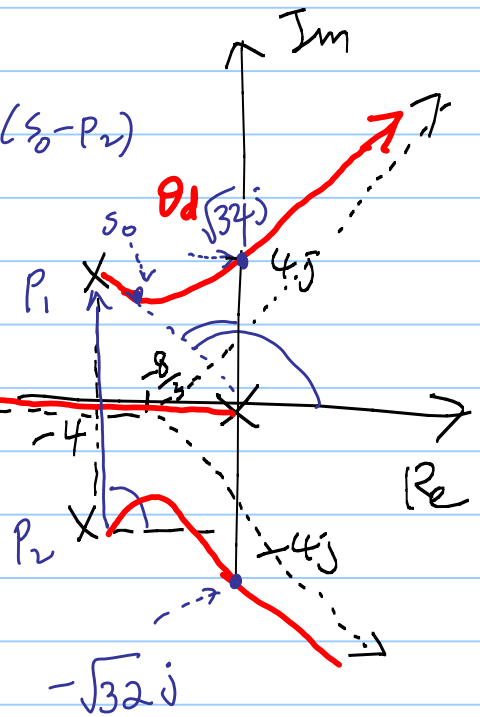
(RL)  $\rightarrow$  Angle condition

$$\angle L(s_0) = \angle 1 - \angle s_0 - \angle (s_0 - P_1) - \angle (s_0 - P_2) = \pm 180^\circ$$

$$\lim_{s_0 \rightarrow P_1} \angle L(s_0) = -\angle P_1 - \lim_{s_0 \rightarrow P_1} \angle (s_0 - P_1) - \angle (P_1 - P_2)$$

$$= -135^\circ - \theta_{dep} - 90^\circ = \pm 180^\circ$$

$$\theta_{dep} = 180^\circ - 90^\circ - 135^\circ = 90^\circ - 135^\circ = -45^\circ$$



$$s = j\omega$$

$$CE \quad 1 + KL(s) = 0$$

$$CE. \quad s^3 + 8s^2 + 32s + k = 0$$

$$1 + \frac{k}{s[s^2 + 8s + 32]} = 0$$

$$(j\omega)^3 + 8(j\omega)^2 + 32(j\omega) + k = 0$$

$$\underbrace{(-8\omega^2 + k)}_{=0} + \underbrace{(-\omega^3 + 32\omega)}_{=0} j = 0$$

①

②

$$\text{From } ② \Rightarrow \omega(\omega^2 - 32) = 0$$

$$\omega = \pm \sqrt{32}$$

From ①

$$k = 8\omega^2$$

$$= 8(32) = 256$$