

(P3.1)

(a) the number of microstates is  $2^N$  (pg 91, typo in given answer, printings 1-3)

(b) 3 particles total

$$\Rightarrow P_{\{2H,1T\}} = \frac{3!}{2!*1!} = 3 \text{ number microstates of specific arrangement (macrostate)}$$

probability = (# microstates of specific arrangement)/(total # of microstates)

$$prob = \frac{3}{2^3} = \frac{3}{8}$$

(c) # microstates.

$$P_{\{2H,2T\}} = \frac{4!}{2!*2!} = 6$$

$$P_{\{3H,2T\}} = \frac{5!}{3!*2!} = 10$$

$$P_{\{4H,2T\}} = \frac{6!}{4!*2!} = 15$$

$$P_{\{3H,3T\}} = \frac{6!}{3!*3!} = 20$$

(d)

macrostate		# of microstates*
H	T	
0	8	1
1	7	8
2	6	28
3	5	56
4	4	70
5	3	56
6	2	28
7	1	8
8	0	1

$$* \text{ number of microstates} = \frac{8!}{m!(8-m)!}$$

total number of microstates is  $2^8 = 256$ , which is the same as the sum from the table.

portion of microstates (probability) for requested configurations:

$$\{5:3\} = 56/256 = 0.219 = 22\%$$

$$\{4:4\} = 70/256 = 0.273 = 27\%$$

$$\{3:5\} = 22\% \text{ like } \{5:3\}$$

$$\text{probability of any one of the three most evenly distributed states} = 22\% + 27\% + 22\% = 71\%$$

(e) for 8 particle system, Stirling's approx will not apply

$$\Delta S/k = \ln(p\{4:4\}/p\{5:3\}) = \ln(70/56) = 0.223$$

(P3.3) 15 molecules in 3 boxes, molecules are identical

$$p_j = \frac{N!}{\prod_{i=1}^3 m_{ij}!} \dots\dots\dots \text{Eqn. 3.4}$$

$$p_1 = \frac{15!}{9!4!2!} = 75075$$

$$p_2 = \frac{15!}{(5!)^3} = 756756$$

$$\frac{\Delta S}{k} = \ln \left[ \frac{p_2}{p_1} \right] = 2.31$$

(P3.4) two dices.

$$\frac{\Delta S}{k} = ?? \quad \text{for going from double sixes to a four and three.}$$

$\Rightarrow$  for double sixes, we have probability of 1/6 for each dice.

$$\Rightarrow p_1 = \left( \frac{1}{6} \right) * \left( \frac{1}{6} \right)$$

for one four and one three  $\Rightarrow$  probability applied for 1/6 for each one in each dice,

$$\Rightarrow p_2 = \left( \frac{1}{6} \right) * \left( \frac{1}{6} \right) * 2$$

$$\frac{\Delta S}{k} = \ln \left( \frac{p_2}{p_1} \right) = \ln 2 = 0.693$$

(P3.5)  $\Delta S = ??$

Assume Nitrogen is an Ideal gas  $\Rightarrow PV = RT \dots\dots\dots \text{Eqn. 1.15}$

$$\Rightarrow P_1 = \frac{8.314(\text{cm}^3 * \text{MPa} / \text{mole} - \text{K}) * 300\text{K}}{23(\text{L} / \text{mole}) * (1000\text{cm}^3 / 1\text{L})} = 0.108\text{MPa}$$

Similarly  $\Rightarrow P_2 = 0.00723\text{MPa}$

$$\Delta S = Cp \ln \frac{T_2}{T_1} - R \ln \frac{P_2}{P_1} \dots\dots\dots \text{Eqn. 3.23}$$

$$Cp = \frac{7R}{2} \dots\dots(\text{ig})$$

$$\Delta S = \frac{7R}{2} * \ln \frac{400}{300} - 8.314 * \ln \frac{0.00723}{0.108} = 30.88\text{J} / \text{mole} - \text{K} = 1.07\text{kJ} / \text{kg} - \text{K}$$

(P3.6) (a) m-balance:  $dn^{in} = -dn^{out}$

S-balance:

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### Chapter 3 Practice Problems

$$\frac{d(nS)^{in}}{dt} = -S^{out} \frac{dn^{out}}{dt} \Rightarrow n^{in} dS^{in} + S^{in} dn^{in} = -S^{out} dn^{out}$$

But physically, we know that the leaking fluid is at the same state as the fluid in the tank; therefore, the S-balance becomes:

$$(ndS + Sdn)^{inside} = -(Sdn)^{out}, \text{ and } dn^{inside} = -dn^{out} \text{ so } \Delta S = 0$$

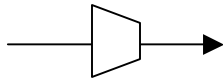
from the steam table .

State	P(Mpa)	T°C	H(kJ/kg)	S(kJ/kg*K)
1(in)	1	400	3264.5	7.4669
2 (out)	0.1	<b>120.8</b>	2717.86	7.4669

At 1 bar =	0.1 MPa
T	S
100	7.361
<b>120.8</b>	<b>7.4669</b>
150	7.6148

By interpolation, implies **T = 120.8°C**

(P3.7) (a) Steady-state flow,  $\Delta H = W_s$



Start 1 mole basis:

$$x_1 = 0.333, x_2 = 0.667, \text{adiabatic}, Cp = x_1 Cp_1 + x_2 Cp_2, \text{ Cp for each is the same anyway.}$$

$$MW = x_1 MW_1 + x_2 MW_2 = 0.333(12 + 16) + 0.667 * 2 = 10.66(g / mole)$$

$$R = 1.987 \text{ BTU/lbmol-R.}$$

$$\Delta H = W_s = \int_{T_1}^{T_2} Cp dT = \frac{7}{2} * R * (1100 - 100)^\circ R$$

$$\Rightarrow \Delta H = 6954.5 \text{ BTU / lbmol}$$

$$\& \dot{m} = 1 \text{ ton / h} = 2000 \text{ lb / h.}$$

$$\& MW = 10.66 \text{ lb / lbmol}$$

$$\Rightarrow \Delta H = \frac{2000 \text{ lb}}{\text{h}} * \frac{\text{lbmol}}{10.66 \text{ lb}} * \frac{6954.5 \text{ BTU}}{\text{lbmol}}$$

$$\Rightarrow \Delta H = W_s = 1,305,000 = 1.3 * 10^6 \text{ BTU / h}$$

(b)  $\eta = ??$  of the compressor.

To find the efficiency of the compressor,  $\Rightarrow S_1 = S_2$

But the enthalpy and the internal energy will change which gives a change in the

$$\text{Work. } \Rightarrow \eta = \frac{W_s'}{W_s} = ??$$

Chapter 3 Practice Problems

$$\Delta S = 0 = C_p \ln \frac{T_2'}{T_1} - R \ln \frac{P_2}{P_1}$$

$$\Rightarrow C_p \ln \frac{T_2'}{T_1} = R \ln \frac{P_2}{P_1}$$

$$\Rightarrow \left( \frac{T_2'}{T_1} \right)^{C_p} = \left( \frac{P_2}{P_1} \right)^R$$

$$\Rightarrow T_2' = \left( \frac{P_2}{P_1} \right)^{\frac{R}{C_p}} * T_1$$

$$\Rightarrow T_2' = \left( \frac{100}{5} \right)^{\frac{2}{7}} * 559R$$

$$T_2' = 1315R$$

$$\& \Delta H' = C_p(T_2' - T_1) = 6.95(1315 - 559) \Rightarrow \eta = \frac{\Delta H'}{\Delta H} = \frac{5258}{6955} = 0.76$$

$$\Rightarrow \Delta H' = 5258 \text{ BTU} / \text{lbmol}$$

(P3.8) Adiabatic, steady-state open system  $\Rightarrow Q = 0$ , &  $(C_p/R = 7/2)$ ..... ig

$$W = \int_{300}^{625} C_p dT = \frac{7R}{2} * (625 - 300) = 9457.175 \text{ kJ} / \text{kmole} * \frac{1 \text{ kmole}}{28 \text{ kg}} = 337.76 \text{ kJ} / \text{kg}$$

$\eta = ??$

$$\Delta S = 0 \Rightarrow \frac{T_2'}{T_1} = \left( \frac{P_2}{P_1} \right)^{\frac{R}{C_p}}$$

$$\Rightarrow T_2' = 533.5 \text{ K}$$

$$\Rightarrow \Delta H' = C_p(T_2' - T_1) = \left( \frac{7 * 8.314}{2} \right) * (533.5 - 300)$$

$$\Rightarrow \Delta H' = 6794.77 \text{ kJ} / \text{mol}$$

$$\Rightarrow \eta = \frac{\Delta H'}{\Delta H} = \frac{6794.77 \text{ kJ} / \text{kmol}}{337.76 \text{ kJ} / \text{kg} * 28 \text{ kg} / \text{kmol}} = 0.718$$

$$\Rightarrow \eta = 71.8\%$$

(P3.9) work required per kg of steam through this compressor?

By looking at the steam table in the back of the book

P(MPa)	T(°C)	H(kJ/kg)	S(kJ/kg-K)
0.8	200	2839.7	6.8176
4	500	3446	7.0922

$$W = \Delta H = 3446 - 2839.7 = 606.3 \text{ kJ} / \text{kg}$$

now find  $W' = ??$

### Chapter 3 Practice Problems

$\Delta S = 0$  (reversible),  $\Rightarrow$  look in the steam table (@P = 4.0MPa) to find a similar value for  $S = 6.8176$ kJ/kg-K, if this value is not available so find it by interpolation.

H(kJ/kg)	S(kJ/kg-K)
3214.5	6.7714
H' = ??	S' = 6.8176
3331.2	6.9386

$$\Rightarrow \frac{3331.2 - H'}{3331.2 - 3214.5} = \frac{6.9386 - 6.8176}{6.9386 - 6.7714}, \Rightarrow H' = 3246.7$$

$$\Rightarrow \Delta H' = W' = 3246.7 - 2839.7 = 407 \text{ kJ / kg}$$

$$\Rightarrow \eta = \frac{407}{606.3} = 0.67, \Rightarrow \eta = 67\%$$

(P3.10) @ P = 2.0 MPa & T = 600°C,  $\Rightarrow H = 3690.7$  kJ/kg, S = 7.7043kJ/kg-K (Steam table)

	T(°C)	H <sub>L</sub> (kJ/kg)	$\Delta H^{\text{vap}}$ (kJ/kg)
steam table	20	83.91	2453.52
<b>Interpolation</b>	<b>24</b>	<b>100.646</b>	<b>2444.098</b>
steam table	24	104.83	2441.68

$$H = H_L + q(\Delta H^{\text{vap}}) = 100.646 + 0.98 * (2441.68) = 2493.49 \text{ kJ / kg}$$

$$\Rightarrow W_s = \Delta H = 3690.7 - 2493.49 = 1197.21 \text{ kJ / kg}$$

$$\eta = ??, \quad \eta = \frac{\Delta H}{\Delta H'} = \frac{W}{W'}$$

$\Rightarrow \Delta S = 0$  (reversible),  $\Rightarrow$  look for S in the sat'd temp. steam table and find H by interpolation,  $\Rightarrow W' = 1408.0 \text{ kJ / kg}$

$$\Rightarrow \eta = \frac{1197.2}{1408.0} = 0.8503, \Rightarrow \eta = 85\%$$

(P3.11)

$$P_1 = 0.1 \text{ MPa, Sat'd } d_{\text{vap}}$$

$$P_2 = 10 \text{ MPa}$$

$$T_2 = 1100^\circ \text{ C}$$

State	P(MPa)	T(°C)	H(kJ/kg)	S(kJ/kg-K)
1	0.1	99.61	2674.95	7.3589
2'	10		<b>4062.53</b>	7.3589
2	10	1100	4870.3	8.0288

interpolation for above table:

Chapter 3 Practice Problems

$H'_2 = 4062.53$	(interpolation)
<b>H(kJ/kg)</b>	<b>S(kJ/kg-K)</b>
3992	7.2916
<b>4062.53</b>	<b>7.3589</b>
4114.5	7.4085

$$\Rightarrow \Delta H = W_s = 4870.3 - 2674.95 = 2195.35 \text{ kJ/kg}$$

mass flow rate = 1 kg/s

$$\Rightarrow \dot{W}_s = 2195.35 \text{ kJ/s} = 2195350 \text{ watt}$$

$$\& 1 \text{ watt} = 0.001341022 \text{ hp}$$

$$\Rightarrow \dot{W}_s = 2944.01 \text{ hp}$$

$$\& \Delta H' = 4062.53 - 2674.95 = 1387.58 \text{ kJ/kg}$$

$$\Rightarrow \eta = \frac{\Delta H'}{\Delta H} = \frac{1387.58}{2195.35} = 0.63$$

$$\Rightarrow \eta = 63.2\%$$

(P3.13) Through the valve  $\Rightarrow H^{in} = H^{out}$

$$P^{in} = 3 \text{ MPa} \quad P^{out} = 0.1 \text{ MPa} \quad T_{out} = 110^\circ \text{C} = 383.15 \text{ K}$$

(By interpolation) Find  $H^{out}$  from steam table.

$$\frac{150 - 110}{150 - 100} = \frac{2776.6 - H^{out}}{2776.6 - 2675.8}$$

$$\Rightarrow H^{out} = 2695.96 \text{ kJ/kg}$$

At 3 MPa table use same value for  $H^{in}$  to find  $S^{in}$

$$\Rightarrow \text{By interpolation } \frac{2856.5 - 2695.96}{2856.5 - 2803.2} = \frac{6.2893 - S^{in}}{6.2893 - 6.1856}$$

$$\Rightarrow S^{in} = 5.976 \text{ kJ/kg-K}$$

The process should be irreversible. To find  $S^{out}$ , interpolate using temperature at 0.1 MPa:

$$\frac{150 - 110}{150 - 100} = \frac{7.6148 - S^{out}}{7.6148 - 7.3610}$$

$S^{out} = 7.4118 \text{ kJ/kg-K}$ , since  $S^{out} > S^{in}$  entropy has been generated. The entropy balance is:

$$0 = S^{in} \dot{m}^{in} - S^{out} \dot{m}^{out} + \dot{S}_{gen}$$